

# Application of Latent Change Score Models to Study Specific Changes

## Introduction

### Motivation

- Latent growth curve models (LGCs) examine the “average rate of change” over the entire study period. However, *change in a specific time interval* could be the actual research interest.
- Studying “specific change” can inform:
  - Change in each time interval
  - When a substantial change occurs
  - How long the substantial change continues for

### Purpose of study

- To introduce the application of latent change score (LCS) model to examine:
  - Change from a previous time point
  - Change from the baseline (first time point)
  - Change from a particular time point of interest

## Illustration with Depressive Symptoms Scale

### Samples and measures

- 494 high school students in Vancouver
- The depressive symptoms scale (Bosworkth, Espelage, & Dahlberg, 1996)
- Outcome (range 1 to 5) was measured over 3 years

### Research questions

- How had depressive symptoms changed from previous year?
- When did depressive symptoms show a substantial change from the baseline? And, how long had the change continued for?

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## REFERENCES

- McArdle, J. J., & Hamagami, F. (2001). Latent difference score structural models for linear dynamic analyses with incomplete longitudinal data. In L. M. Collins & A. G. Sayer (Eds.), *New methods for the analysis of change* (pp. 139–175). Washington: American Psychological Association.
- Bosworth, K., Espelage, D., DuBay, T., Dahlberg, L.L., & Daytner, G. (1996). Using multimedia to teach conflict resolution skills to young adolescents. *American Journal of Preventive Medicine*, 12, 65–74.

## A Proportional Change Model and its Extensions for Studying Specific Changes

### Proportional Change Model, a type of LCS model (McArdle & Hamagami, 2001)

- LCS models examine a change based on latent difference scores. An individual’s true score at each time point is modeled as a sum of previous true score and *the difference score (i.e., change)*.

$$Y_{ti} = Y_{(t-1)i} + \Delta Y_{ti}, \quad (1)$$

where  $Y_{ti}$  is the true score at time  $t$  for individual  $i$ ,  $Y_{(t-1)i}$  is the true score at time  $t-1$  (i.e., previous time), and  $\Delta Y_{ti}$  is the latent difference score between time  $t-1$  and time  $t$ .

- A *proportional change model* addresses *interval specific difference scores* and is especially flexible for examining specific changes between time points.

### Change from a previous time point to next time point

- A proportional change model shows a change for each time interval as follows:

$$\Delta Y_{ti} = \beta_{ti} * Y_{(t-1)i} \quad (2)$$

$$Y_{ti} = Y_{(t-1)i} + \beta_{ti} * Y_{(t-1)i} \quad (3)$$

$\Delta Y_{ti}$  is the latent difference score between true scores at time  $t$  and its previous time point  $t-1$ .  $\beta_{ti}$  expresses the change as a proportion of previous true score.

### Change from the baseline (first) time point to each time point

- The proportional change model can be extended to examine changes from the baseline by expressing true scores at time  $t$  as a sum of baseline and the difference between the baseline and time  $t$ :

$$\Delta Y_{ti} = \beta_{ti} * Y_{(baseline)i} \quad (2a)$$

$$Y_{ti} = Y_{(baseline)i} + \beta_{ti} * Y_{(baseline)i} \quad (3a)$$

$\Delta Y_{ti}$  is the latent difference score between true scores at time  $t$  and the baseline.  $\beta_{ti}$  expresses the change as a proportion of baseline true score.

### Change from a particular time point to each time point

- If the second time point is chosen as a meaningful reference, changes from the second time point can be examined by expressing true scores at time  $t$  as a sum of true score at the second time point and the difference between the second time point and time  $t$ :

$$\Delta Y_{ti} = \beta_{ti} * Y_{(second)i} \quad (2b)$$

$$Y_{ti} = Y_{(second)i} + \beta_{ti} * Y_{(second)i} \quad (3b)$$

$\Delta Y_{ti}$  is the latent difference score between true scores at time  $t$  and the second time point.  $\beta_{ti}$  expresses the change as a proportion of second time point true score.

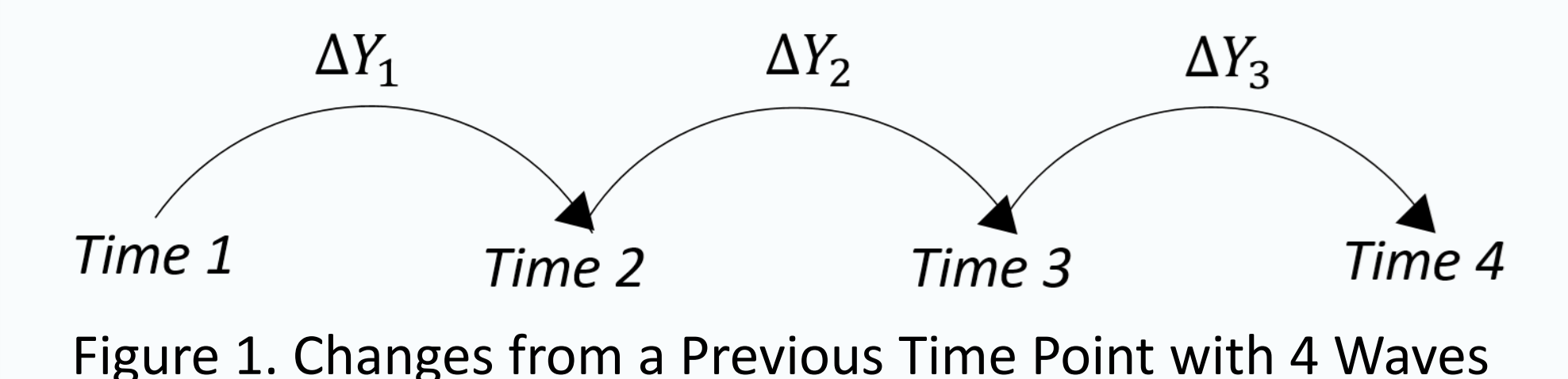


Figure 1. Changes from a Previous Time Point with 4 Waves

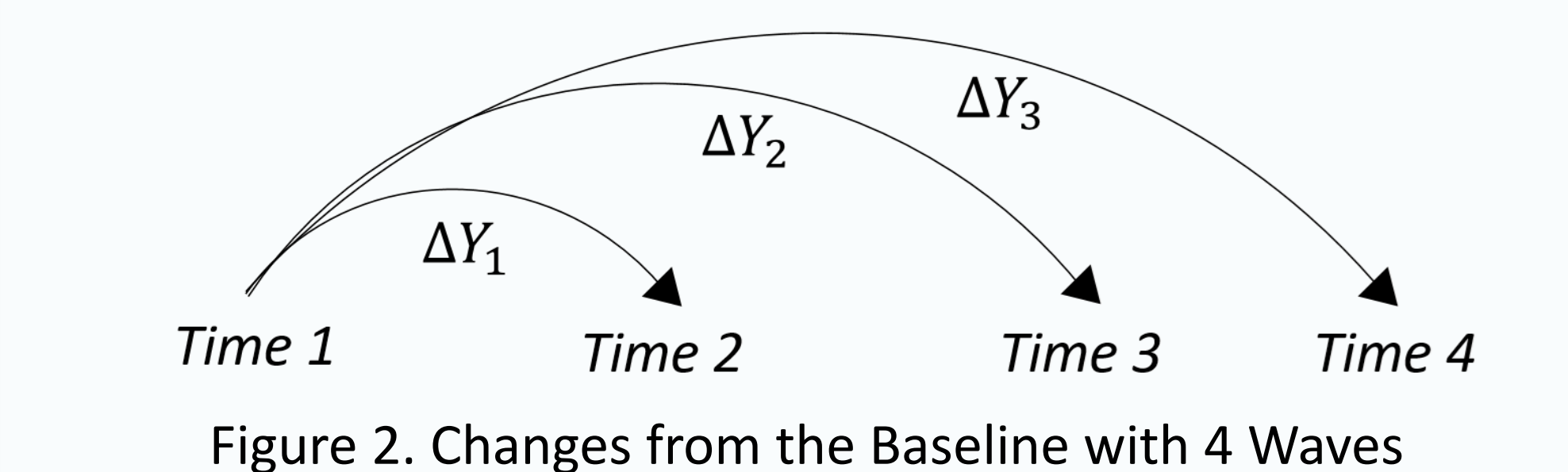


Figure 2. Changes from the Baseline with 4 Waves

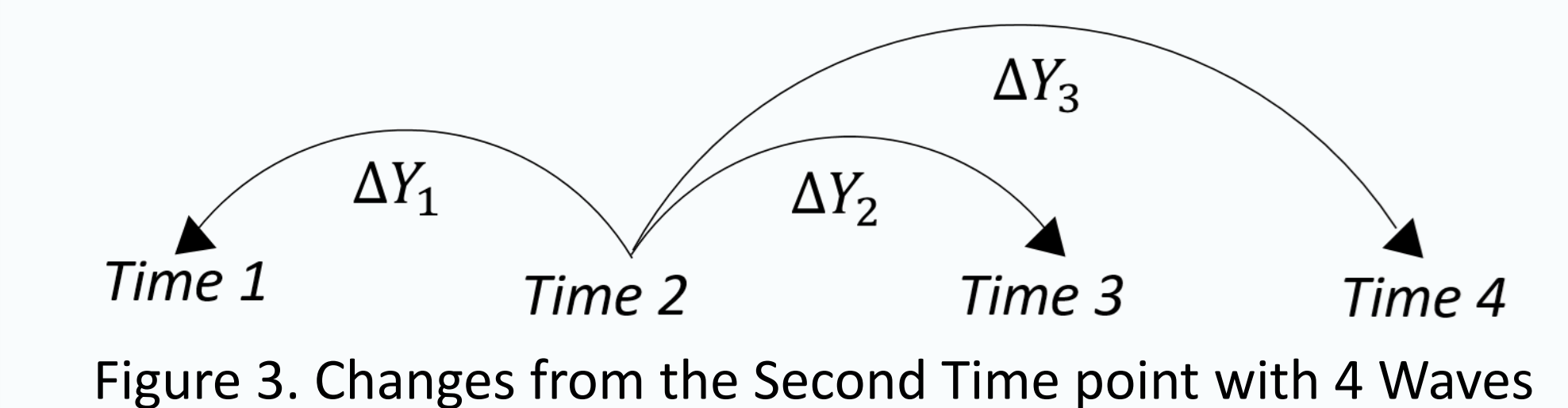


Figure 3. Changes from the Second Time point with 4 Waves

## Results and Implication

### Linear LGCM for average change (Table 1)

- The initial score of depressive symptoms was 2.72 and the score had increased by 0.09 points every year.

### Proportional change model for change from a previous time point (Table 2)

- A 4% significantly increase in depressive symptoms from year 1 to year 2 ( $\beta_1 = 0.04$ ) and a 2% non-significant increase from year 2 to year 3 ( $\beta_2 = 0.02$ )
- It implied that the scores of depressive symptoms increased the most between years 1 and 2, but remained stable afterwards.

### Proportional change model for change from the baseline (Table 3)

- Depressive symptoms in years 2 and 3 were 4% and 6% significantly higher than the baseline ( $\beta_1 = 0.04$  and  $\beta_2 = 0.06$ )
- This indicated that a significant change had occurred during the first time interval, and the change had continued in the following interval.

Table 1. LGCM for Average Change

	Estimate	p
Mean of initial status	2.72 (.03)	<.001
Mean of slope	.09 (.017)	<.001
Variance of initial status	.37 (.04)	<.001
Variance of slope	.05 (.02)	.003

Table 2. Change from Previous Time Point

	Estimate	p
Mean of first time point	2.71 (.03)	<.001
Variance of first time point	.30 (.02)	<.001
$\beta_1$	.04 (.01)	<.001
$\beta_2$	.02 (.01)	.064

Table 3. Changes from Baseline

	Estimate	p
Mean of initial status	2.71 (.03)	<.001
Variance of first time point	.30 (.02)	<.001
$\beta_1$	.04 (.01)	<.001
$\beta_2$	.06 (.01)	<.001

## Discussion

- Studying specific changes in SEM framework has not been discussed often. The proportional change model and its extensions could serve this purpose.
- The proportional change models introduced in this study and LGCs satisfy different research objectives. LGCs are useful to understand “overall” trajectory across time.
- Although results in Table 2 and Table 3 appear very similar, it may not be always the case when the direction of change is inconsistent.